

SYSTEMS ANALYSIS

LECTURE 7

TOOLS

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Lecture overview

- Decision tables
- Cluster analysis
- Graph transmission



Decision tables

Decision tables

- Tool for modeling sets of logical terms
- Similar to if-then rules
- Work with several conditions at the same time
- Advantages
 - ▣ Possibility of modelling complex alternative processes
 - ▣ Suitable for algorithms with many decisions
 - ▣ Easily computerized

Decision tables - structure

- 4 quadrants

List of conditions	Combinations of conditions
List of actions	Combination of actions

- DTs describe which actions are to be done under particular combination of conditions
- In the „Combination of conditions“ quadrant different **possible** combinations of conditions are stated and to each combination there are in the appropriate column in the quadrant „combination of actions“ - markes actions to be done

Decision tables - creating

- 1. Identify conditions and their values
- 2. Identify possible actions
- 3. Enter combinations of conditions
- 4. Define actions for each combination of conditions
- 5. Verify the table and if possible, simplify the table

Example

DS: Should I attend the lecture?				
Was the last lecture useful?	0	0	1	1
Do I have other duties?	0	1	0	1
Stay home and do nothing	1	0	0	0
Work on other duties	0	1	0	1
Attend the lecture	0	0	1	1

- One combination can have more actions
- One action can be done for more combinations of conditions

Types of decision tables

- According the inputs
 - ▣ With limited-entry (binary input)
 - ▣ With extended entry (each condition has more possible results)
 - It is possible to put down the different values (intervals) in the combinations of conditions
 - Or every condition in the first quadrant has as many formulations, as there are possible inputs
 - ▣ With mixed inputs

Example – table with extended entry

DS: Evening activity				
How much money I have at disposal?	<50	50-200	200-500	>500
Stay at home	1	0	0	0
Go to pub	0	1	0	1
Go to a theater	0	0	1	0
Invite friends	0	0	0	1

DS: Evening activity				
I have at disposal <50 Kč	1	0	0	0
I have at disposal 50-200 Kč	0	1	0	0
I have at disposal 200-500 Kč	0	0	1	0
I have at disposal >500 Kč	0	0	0	1
Stay at home	1	0	0	0
Go to pub	0	1	0	1
Go to a theater	0	0	1	0
Invite friends	0	0	0	1

Example – table with contradictory entry

- e.g. choosing signal plan for traffic control

Day: public holiday	1	0	0	0	0
Monday	-	1				
Tuesday	-		1			
Wednesday	-			1		
....	-					
Sunday	-					
Use signal plan A	1					
B		1				
C			1	1		

Types of decision tables

- According cohesion with other DT
 - ▣ Open – there are more DT connected (using links from one to another)
 - ▣ Closed – one self-sustaining table
- Full tables – with limited binary entry, number of rules is 2^n
 - ▣ More often there are less rules because of redundancy or contradictory

Example – open table

DT 1				
Do you have ticket?	0	0	1	1
Do you have cell phone?	0	1	0	1
Go on foot	1	0	0	0
Send SMS	0	1	0	0
Go to DT 2	0	1	0	0
Return from DT 2	0	1	0	0
Get on the vehicle	0	1	1	1

DT 2		
Have you received the SMS ticket?	0	1
Wait - Repeat DT 2	1	0
Return to DT1 and continue	0	1



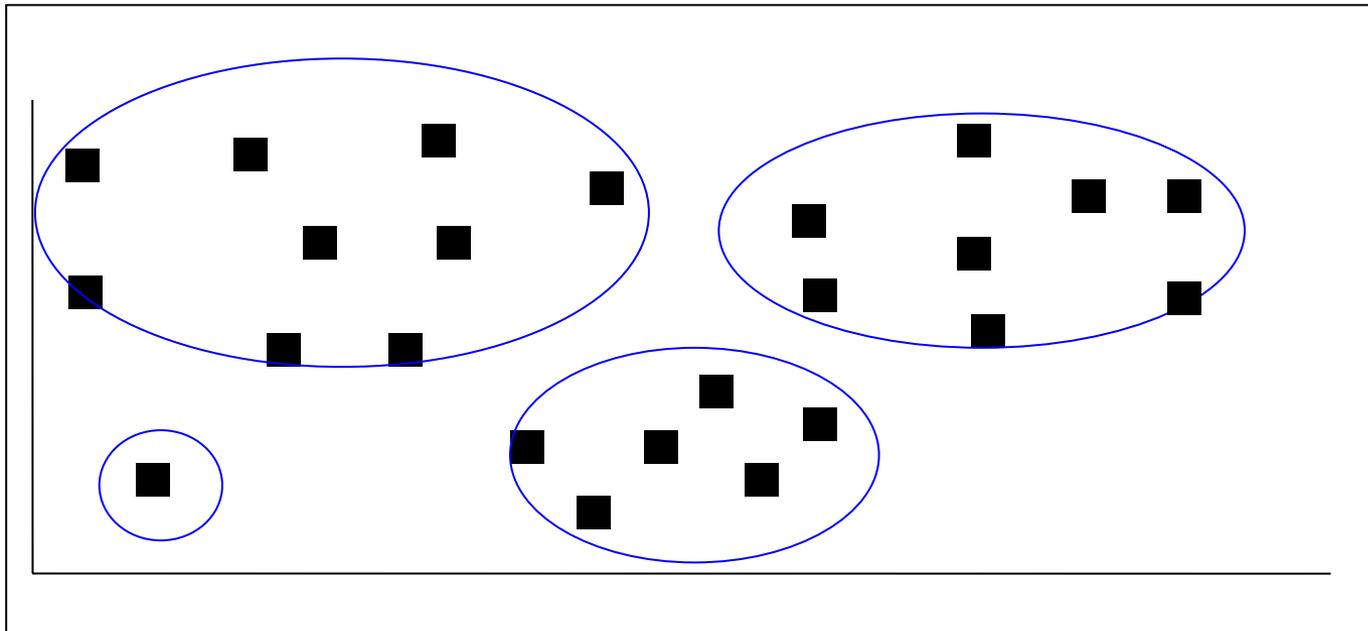
Cluster analysis

Cluster Analysis - CA

- Method for clustering similar objects
- Combines mathematical and expert attitudes

- Usage in the Systems analysis, e.g.
 - ▣ System identification
 - ▣ Semantic decomposition

Example for 2D position

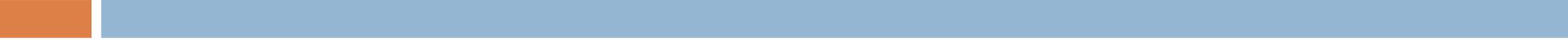


Typical procedure

- Choice of objects (elements) objektů / prvků
- Choice of measured characteristics and assignment of weights to these characteristics
- Choice of measure of similarity of elements – metrics
- Choice of clustering method
- If needed, determination of number of clusters (either based on expertise or using full hierarchical analysis and setting of rules for choice of optimal level)
- Calculation
- Results interpretation

Cluster analysis methods

- E.g.:
 - K-means
 - ISODATA
 - ...



Graph transmission – Mason-Truxal rules

Graph transmission

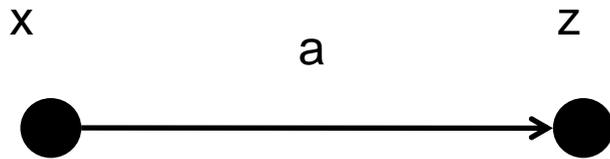
- Procedure of transferring of system of linear equation into a graph (the system matrix must be partially empty) – izomorfism between oriented graph and system of linear equations
- It serves for simple solving of system transmission (proportion of output and input $(x_i \rightarrow x_j)$)

Graph transmission

- Usage
 - regulation
 - Control technique
 - Cybernetics
- Topological or algebraical form
- Topological form – Mason-Truxal rules

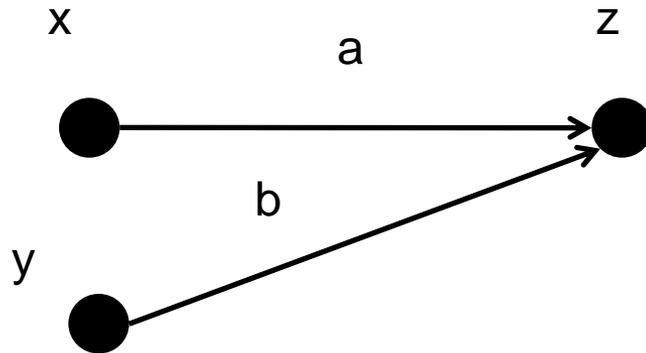
How to transfer the equations into graph

□ $z = a * x$

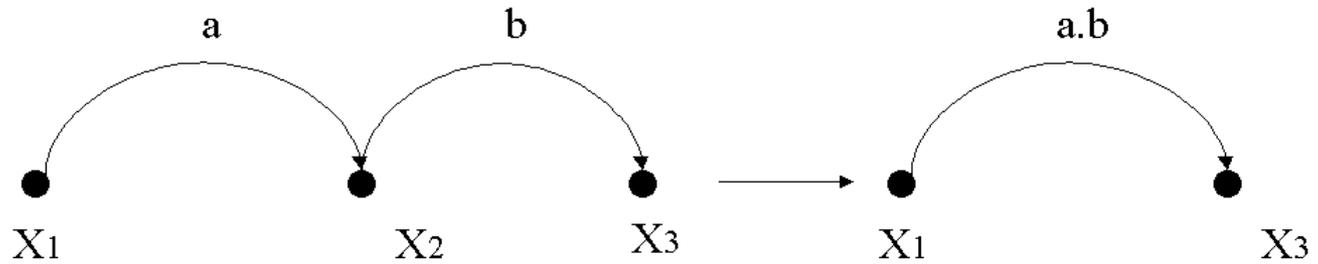
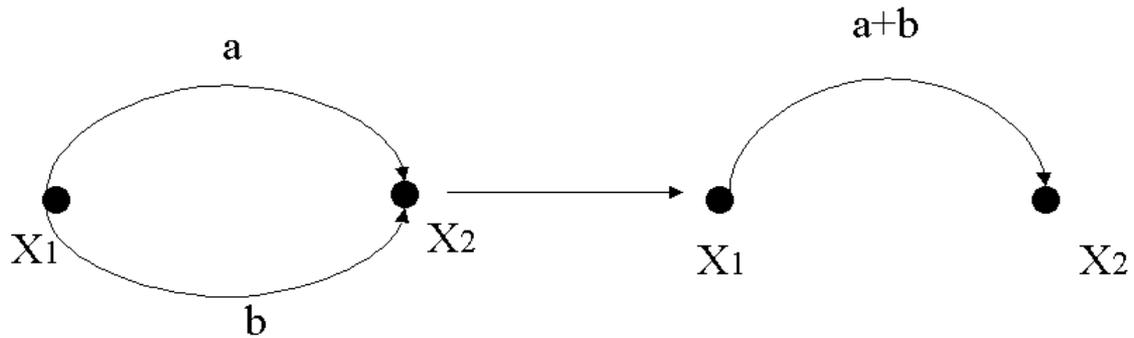


x, y, z – variables
a, b - constants

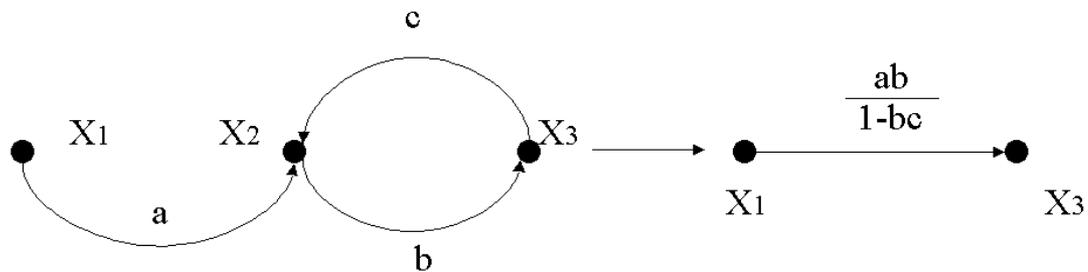
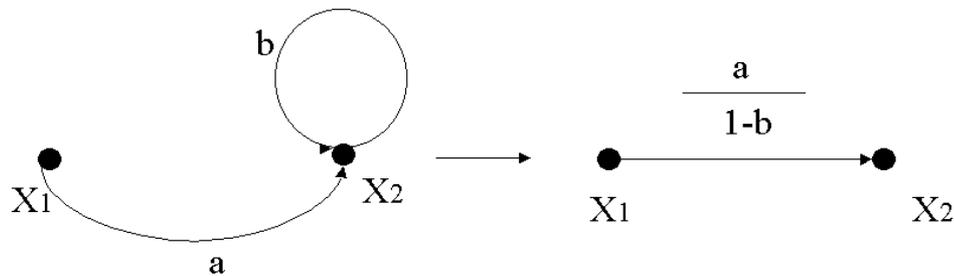
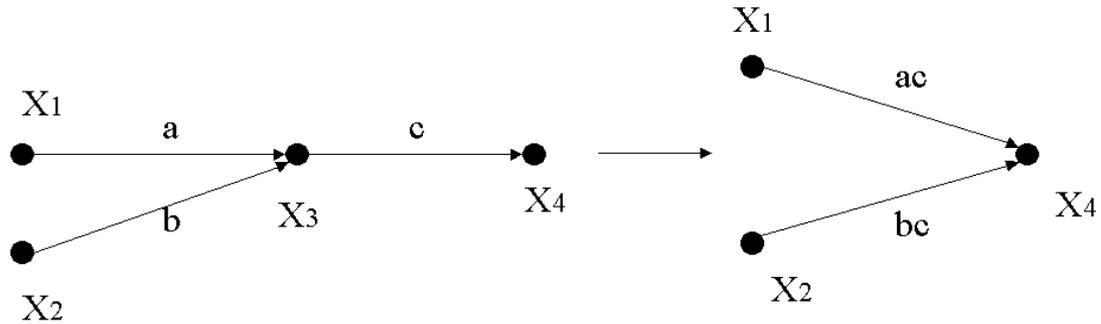
□ $z = a * x + b * y$



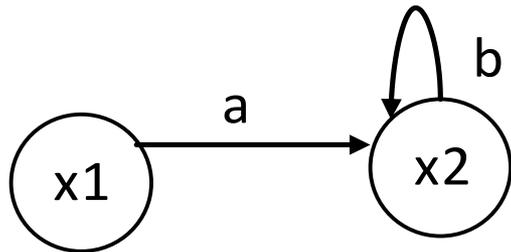
The Mason-Truxal rules I



The Mason-Truxal rules II



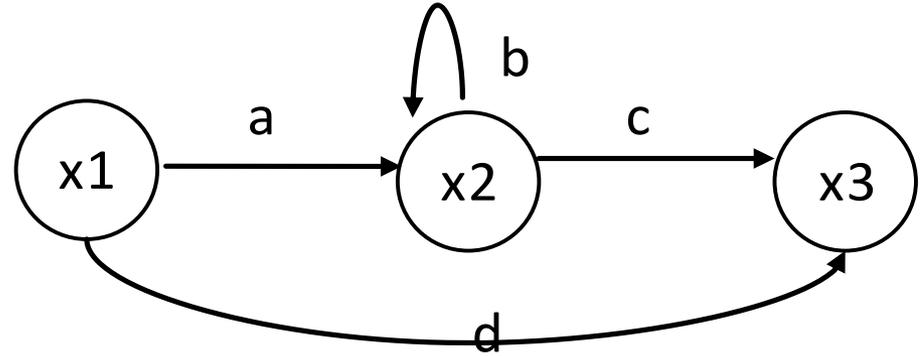
Feedback rules - deduction



- $x_2 = a \cdot x_1 + b \cdot x_2$
- $x_2 = a \cdot x_1 + b \cdot x_2 \quad x_2 - b \cdot x_2 = a \cdot x_1$
- $x_2(1-b) = a \cdot x_1$
- $x_2/x_1 = a/(1-b)$

Example

$$x_2 = a * x_1 + b * x_2$$
$$x_3 = c * x_2 + d * x_1$$



$$\frac{x_3}{x_1} = \left(\frac{a}{1-b} * c \right) + d$$

□ Verification

$$x_2 = \frac{a * x_1}{1-b}$$

$$x_3 = c * \frac{a * x_1}{1-b} + d * x_1$$

$$\frac{x_3}{x_1} = \frac{a * c}{1-b} + d$$

Graph transition - terms

- **Path** – continuous succession of branches, no node is encountered more than once
- **Loop** – simple closed path,
- **Self loop** – loop with no other node than the origin=destination node

Graph transmission – basic rules

- Path transmission = product (multiplication) of all branch transmissions along a single path
- Transmission of parallel paths = sum of the path transmissions of all the possible paths between two nodes
- Absorbing node (not a loop node) – it must be included in all the direct paths going through it
- Absorbing several self-loops of one node into one – sum of the self-loops
- Absorbing self-loop with transmission b – transmission **of every incoming branch** is divided by $(1-b)$

Graph transmission – procedure

- Absorbing nodes with just one input or output
- Absorbing all parallel branches (with the same orientation)
- Absorbing self-loops
- Absorbing loop node – all direct and self paths must go through the node must be assessed

References

- Graph transmission
 - D. Eppinger Murthy V. Nukala Daniel E. Whitney: Generalized Models of Design Iteration Using Signal Flow Graphs Steven. MIT, Sloan School of Management, 1996. Accessible from:
<https://core.ac.uk/download/pdf/4380258.pdf>
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